Non Eq Pt 1 What is Non-Equilibrium Stat Mech? Real & modern non-eg stat mech: Systems w/ dissipation, which means heat/entropy flows in or out ot system I doing or having work done on system, Non adjabatically ] . In many cases, this Means time reversibility in dynamics is broken · Sometimes we can reach a non-exilibrium Stendy state" where there is constant driving but basically at equilibrium Examples: Self assembly by drying/in a field Self driver / externelly driver particles molecular motor (consume ATP to do world) folding / untolding proten under faree...

Some theories have developed to treat these "Eerl" non-cquilibrium Systems All of that is built on understanding dynamics of systems " Near" equilibrium fiest, · Additionally, we have to unelesstand bearn about degranics, especially systems is contect w/a bith & how to study then I time dependent processes ] Back to Brownian motion & origin of Longevin envotion the particle has drag:

I radius m dv = - zv,  $z = 6\pi za$ Stokes law, 3d sphere

If this were whole story then  $U(t) = U(0) e^{-\frac{t}{2}t/m}$  [more day, lighter pertiale

Stops Fisher] This would ment that the particle stops moving But we know (from bosone, also xpts/ that </p [ ('/2mv+7= (ke) = KoT/2] => <v2>=+T/M So this is where we get Canyon's idea of MdV = - GV + SF(H) vonden Larce

flocksting force in each dioechin Assert collisions uncorrelated in fine 8 mea zero < SF(+) >=0 (SF(+) SF(+'))= ZBS(+-+') So how do we solve this exaction? Have to do once by a "frick" for diff ca

$$\frac{dx(t)}{dt} = \alpha x(t) + b(t)$$
in sert  $x(t) = e^{at}y(t)$ 
then  $e^{at}dy(t) + ae^{at}y(t) = ae^{at}y(t) + b(t)$ 

$$= \frac{dy(t)}{dt} = e^{-at}b(t)$$
integrate from  $0 + i \cdot 2$ 

$$y(2) - y(0) = \int_{0}^{2-at}b(t)dt$$

$$x(2) = x(2) = x(2) + \int_{0}^{2-at}e^{-at}b(t)dt$$

$$x(2) = e^{-ax}x(2) + \int_{0}^{2}e^{-at}b(1)dt$$

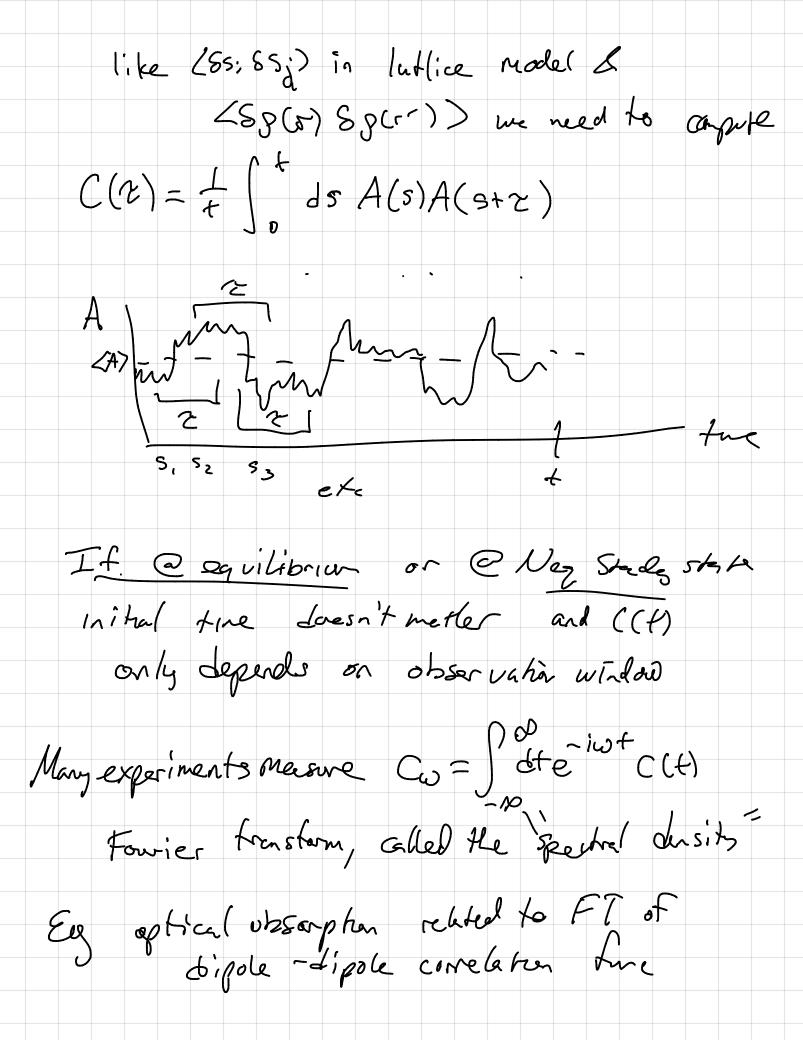
$$x(2) = e^{-ax}x(2) + \int_{0}^{2}e^{-at}b(1)dt$$

$$x(2) = e^{-ax}x(2) + \int_{0}^{2}e^{-at}b(2-3)(1-at)dt$$

$$x(3) = e^{-ax}x(3) + \int_{0}^{2}e^{-at}b(2-3)(1-at)dt$$

=>  $V(t) = e^{-\frac{4}{m}t} V(0) + \int dt e^{-\frac{4}{m}(t-t')} \frac{SF(t')}{m}$ Vow we wont to pedict (Vin) So what is  $(V(t))^2$ ?  $V(t)^2 = e^{-t^2/mt} V(0) + 2e^{-t^2/mt} V(0) \int_0^\infty dt e^{-t^2/m(t-t')} dt = \frac{-t^2/mt}{m}$ + 1 + 1 + 1 + 2 = 2/m[+-+']+(++") = (+') S = (+' 

Time correlation tructions Only one Eq State, but many nonaguilibrium stres there is no (probably) Unique partition Ruetra. What we compute in stend are time correlaction tunetions (more like gCr), but in time) These will correct to: Viscosity, Hemal cond, differsin & Scattering spectroscopy & NMZ Measurements are Still anerages, but now Sceck to time averages  $\langle A \rangle = \frac{1}{2} \int_{0}^{2} dt A(t)$ Fluctuations from men SA(t) = A(H - LA) Fluctuations are correlated in time, so



Example - the correlations in velocity are related to the diffusion const We showed bisussed Diffesion of a perticle in Id, Macrosopically DitPusion is defined 29 or diff Eq railed the diffusion eq D(x,t) is conc at x at time f

D(x,t) = D D(x,t)

St D(x,t) = D D(x,t) if S(x,0) = S(x), spreads out as a garssian  $\omega$ / time,  $\omega$ / (S(x)) = 0what is the MSD (also, the various of this garssim? Stert w/  $(x^2)_{x} = \int_{-\infty}^{\infty} dx x^2 p(x,t)$  $\frac{\partial}{\partial t} \left( \frac{1}{x^{2}} \right)^{2} dx x^{2} \frac{\partial}{\partial t} f(x)(x,t) = \int_{-\infty}^{\infty} dx Dx^{2} \frac{1}{dx^{2}} f(x,t)$   $= D \left[ \left( \frac{1}{x^{2}} \frac{1}{x^{2}} f(x,t) \right)^{\infty} - \int_{-\infty}^{\infty} 2x \frac{1}{x^{2}} f(x,t) dx \right]$   $= D \left[ \left( \frac{1}{x^{2}} \frac{1}{x^{2}} f(x,t) \right)^{\infty} + 2 \int_{-\infty}^{\infty} f(x,t) dx \right] = 27$ 

$$\begin{array}{l} \Longrightarrow \langle x^2 \rangle = 2Dt \\ (showed for discrete conlar walk before) \\ Dot now, Sx(t) = \int_0^t v(s) ds \\ \langle Sx(t)Sx(t)\rangle^2 / (\int_0^t v(s)v(t) ds) \\ \stackrel{d}{=} \langle (Sx(t))^2 \rangle = \langle 2\int_0^t v(s)v(t) ds \rangle \\ = 2\int_0^t \langle v(s)v(t) \rangle ds \\ = 2\int_0^t \langle v(s)v(t) \rangle ds \\ = 2\int_0^t \langle v(s-s)v(t-s) \rangle ds \\ = 2\int_0^t \langle v(s-s)v(t-s) \rangle ds \\ = 2\int_0^t \langle v(t-s)v(t-s) \rangle ds \\ = 2$$