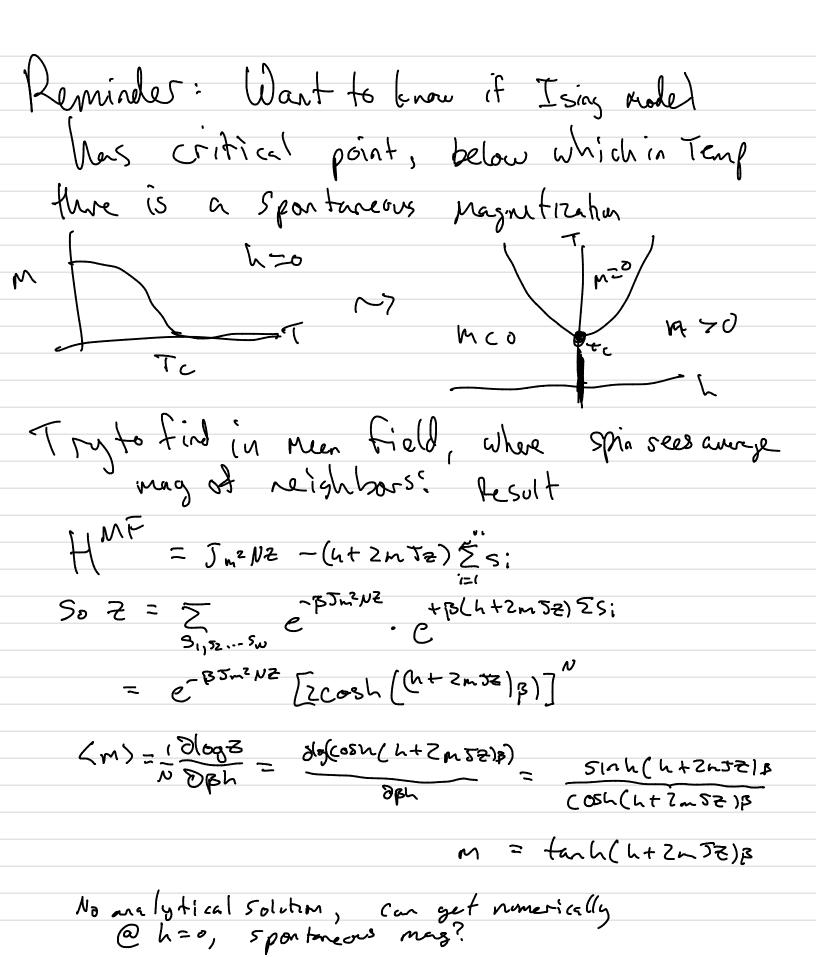
Phose transitions: Part 3

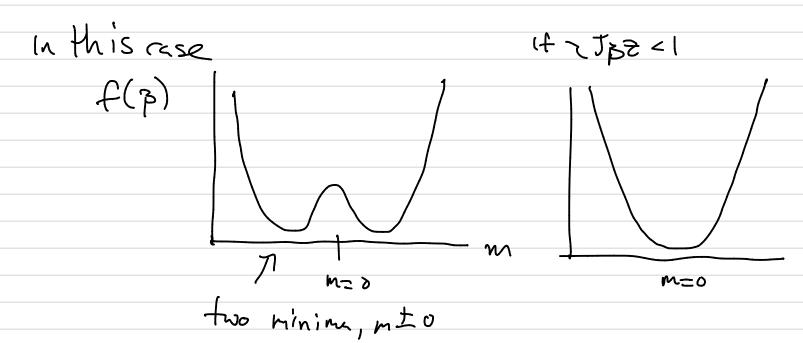


2月ブモ フ1 tenh(273Jm2) 2352<1 tou T, 3 solutions, M=0, trivial not as interesting other solution where lines cross 28JZ=1 separates the regimes, 8 herce KoTc = 2 Je gives predicted critical point For Id, wrong, No To Zo for 2D, Tc = 7.769 J/kg 50 Men field Beter as 2->17, in general Lets-expend f(m, B) near m=0 near B=Bc f(m, p) 2 - kgT log2 = Jm 2 2 - 1 log(2 cosh(4+2m25)p]) 2 (08h (x)= extex 2 [\frac{1}{2} \frac{1

Nevron
$$(65(1+x)=x-\frac{x^{2}+x^{3}}{3}-...$$
So $f(0,\beta)$ ~ $C_{0}+C_{2}x^{2}+C_{4}x^{4}+...$

$$C_{2}=J_{2}+J_{3}$$

Cz = Jz - 25223 reg whn 25223> JZ



In many cases, physicists will posit a free every like this bused on the symmetries of the problem, then predict critical behavior For any problem where, near phase transition f(T) & CI+ Czm2 + cum4 aste une de moro = ZmCz + 4Cym3 => $m_0^2 = -\frac{7c_2}{4Ly} = m_0 \sim \frac{-c_2}{2C_y}$ Bc= 212, Cz= JZ- 2522B = 1 (T_ - Ter) = TC (T-TC) mo~ (T-Tc) 1/2 5 critical exponent B

The behavior new a critical point is very strange, and involves many properties
"diversing," meaning they become in finitely longer
as one got close to the transition

We can characterize the townsition we are observing by its coitical exponents, the power of the dinergence, ie this p. What nakes place transitions forscinating is the Universality, Seemingly different problems had/have some erition openents, in perticular $CU \sim |T-TC|^{-\chi}$, $C_{V} = (\frac{\partial E}{\partial T})$ $K_{T} \sim |T-TC|^{-\chi}$, $k_{T} = -\frac{1}{V}(\frac{\partial V}{\partial T})$ P-Pc~(p-yc) 5 (gn (p-pc) S.-56 ~ |T,-T/B

Table 16.1 compares ising model to gas, liquid Securityly some exponents KT~ X= 3m/3h P~ h= 2A/SM (v ~ Cv Cnot shown, Di-80 ~ m) Scientists started to notice this believier and in the mid 60's, theories stated to emerge or the orisin of these trends widon was abke to derive corrections between the exponents by a scaling theory, Mening (solving at how the free energy Charges w/ Hermodyhanic purameters Eg Z-X=ZB+& [saling relation] [maybe next class] Thisalso follows from trenomalization goog theory r. Thrus out x = C [see 19622] real dz. 1, \$ = -34, \$ = 1.35, 6=4.2

These systems have some critical expensits because they are in the some universality class and have same types of symmetres: The things that ead up mattering are: 1) Dimension of order parameter (n) Magnetization/density = Scalar, n=1 2) Dinersian in which the system lines: ie 3d ising model/ liquid gas, d=3 Men field models give result for d-700 eg in MFT, n=1, we saw \$= 1/2 Another example: m= tanh (R(Justh))

h=ksttanh (m)-2m Jt (like presure) expending wr Tanh n x + x3/3 + ... necr m=0

2 week h~kBt (m+ m3/3/ 2h52 = mkg(T-252/K) + kgT/3 m3 = mkg (T-Tc) + ksT m3 50 h~m3, S=3 2 = Danger = Johjan Dh/om ~ kg (T-Tc) + KoTm² for T>Tc, m=0, so us $\lim_{T\to T_c^+} \chi = \frac{1}{k_0(T-T_c)} \alpha \left(T-T_c\right)^{-1}$ 50 8=1