Phase transitions: Part 1

We are all very familiar w/ Phense transitions in our day to day life, but we don't always think about Many interesting aspects 1) What is hypering Microscopically 2) What is happening Marcroscopically 3) how many pluse transitions have "minusal" properties that don't depend on the specific system This is what has fascinated people from stat mich far ~100 years 4 mijer modern aveas at work! 1) How to sample / observe / predict pleases in smulation 2) What hypers in unusual environments, eg w/ confinement (water in a nanetube, protein...) 3) what is place drasma for many components (inpide...) 4) What happens out of equilibrium? We have to start w/ the basics de understand the more complex plenomena

freeze / crystallize (Tudermen Chyter 16) Basic Pluse P Diagran Solid liquid 4 conduse Jupprile d position Cross a line, discontinuity in some grantity! e.g. densily Elvenfest: discontinuity in deriv. of free energy [density ~ /(0+ 3P) Modern definition: has to be latert hat at cossing C For right, can go between pluses w/or latent heart or weird behavior. C Critical point: 2nd order place Donsition Charge in Second Deriv, but dision times Madern! "Continious" phese transition, diversing sicceptibility, powerlaw driverence of correlation length CDiscuss man later 3 Typically, brack symmetry in 1 direction Liquid -> solid, translational Symmetry, Liquid -> gas Ocorrelation length -> finite correlation (gbr))

Need model systems to analyze to illustrate the important concepts and which can be "solved for the computer or on poper Magnetilation Phenomenon: Spins on lettice, like being in same direction but entropy prements ordering. Lower Tor increasing B field has ordering Transition Need 'arder parameter" to describe a pluse transition, a quantity that distinguishes the physes. P-Pr works for Liquid gas as Liquid solid, O when a hiquid, nonzero oflerwise Here $M = \left| \left< \sum_{i=1}^{N} \sigma_i \right> \right| \quad m = M/N$ is Mayne fization M Tc "sporteneous megnetization" To is curie temp, Pierre Currie studied this transition Can we "durine" this result. There to start w/ Kamiltonian in canonical ensemble and get Z(N, V, T) to compute M

in Zd: interface hypically of size N'12 and this is big enough cost to 111111. TTTTTT Stubilize ordered State (Usar fire fersion") Still an learn a lot from 1d ising malel, including Mapping all sorts of physical problems to it, like adsorption to a surface, or folding of poptides So what is $Z(N_1U,T)$? Lets rewrite $H = -J ZS_1S_1 + h ZS_2$ i=1we can add periodic boundary carditris, 5NH = 5, and write in a more symmetric way $\mathcal{H} = -5 \sum_{i=1}^{N} S_{i} S_{i+1} - h \sum_{i=1}^{N} (S_{i+1} + S_{i+1})$ $= \sum_{i=1}^{N} \left(-\Im_{S_{i}}^{i} + \sum_{i=1}^{N} (S_{i}^{i} + S_{i}^{i} + 1) \right)$ Z= 2 e-360

= = = = ... Z exp(+p Z (Jsisi+ + 2(si+si+1)) s, s, s, sN i=1 for h=0 = Z C C ... C SI,52,...,5N Defect Let 5, '= 5; 5;-,, can only be = 1, but Zways

 $= 2 \frac{2}{2} e^{\beta J \sigma'_{i}} = 2 \left(\frac{2}{2} e^{\beta J \sigma} \right)^{N} = 2 \left(e^{\beta J} + e^{-\beta J} \right)^{N}$ $= 2 \left(2 \cos h(\beta J) \right)^{N}$

f = F/N= ~ kBT/N loy 2 = - B log [2000h (B5)] + const